

**Wireless Connectivity:  
An Intuitive and Fundamental Guide**

**Chapter 2: Random Access:  
How to Talk in Crowded Dark Room**

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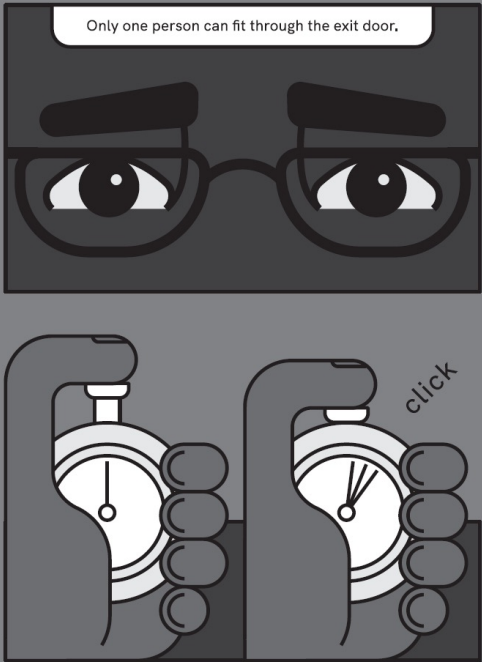
Robin J. Williams



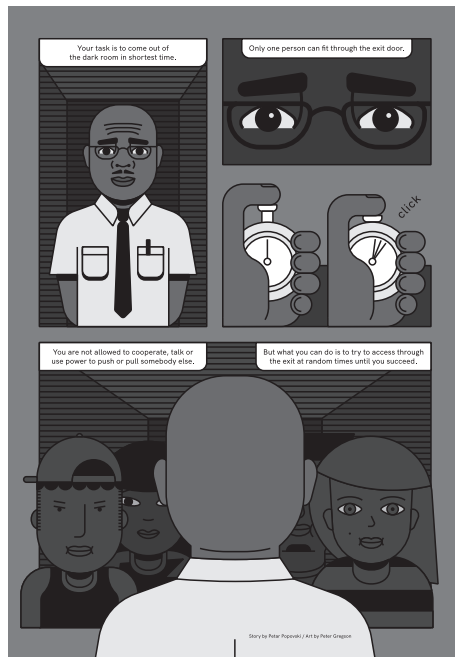
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# Chapters

1. An Easy Introduction to the Shared Wireless Medium
- 2. Random Access: How to Talk in Crowded Dark Room**
3. Access Beyond the Collision Model
4. The Networking Cake: Layering and Slicing
5. Packets Under the Looking Glass: Symbols and Noise
6. A Mathematical View on a Communication Channel
7. Coding for Reliable Communication
8. Information-Theoretic View on Wireless Channel Capacity
9. Time and frequency in wireless communications
10. Space in wireless communications
11. Using Two, More, or a Massive Number of Antennas
12. Wireless Beyond a Link: Connections and Networks



# The essential properties of a random access setup



- Randomized transmission decisions
- The problem of initial access:
  - Could be solved trivially if Walt uses the names of the people in the room to coordinate them
  - When the names are unknown, randomized distributed algorithm should be used
- Efficiency problem when the set of potentially active transmitters is large; the set of actually active transmitters is small and unknown

# What will be learned in this chapter

- When and why to use random access over a shared communication medium
- (framed) ALOHA protocol and the main ideas behind its analysis
- Probing over a shared channel and its connection to group testing
- Carrier sensing: how to take an advantage of a short (cheap) idle slot
- Random access in multi-hop scenario, hidden and exposed terminals

# Canonical scenario for random access

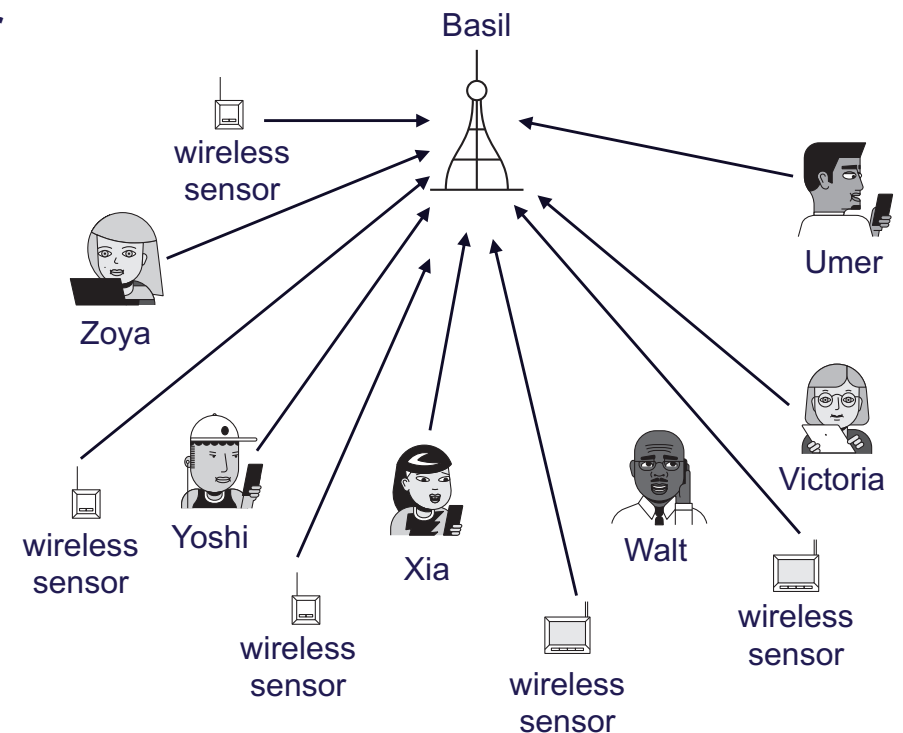
Assume that Basil is in a dark room and other people in that room want to talk to him

- Dark room = same channel for communication (data) and coordination (metadata)

Techniques discussed last time work very well for **deterministic traffic**, especially in the downlink

## Problems

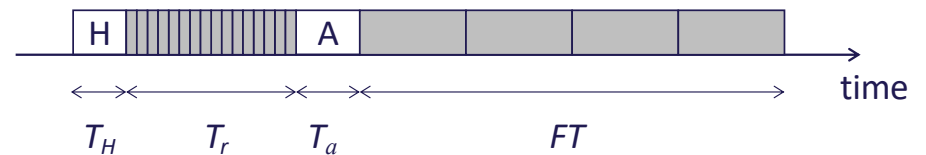
- Initial access
- Lack of coordination in the uplink



# Basic tradeoffs in random access

Scenario with  $K \gg 1$  devices  
out of which only **very few**  
have data to send at a given time

- Basil does not know  
who will be active at a specific time



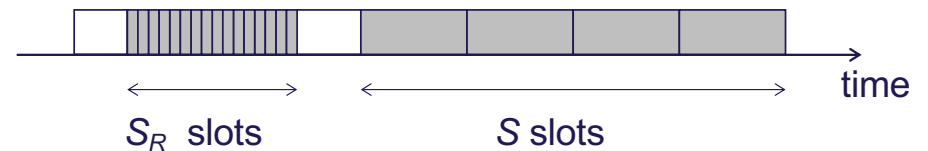
## Tradeoffs

- Allocating an exclusive slot to each of the  $K$  devices may lead to idle (wasted) resources
- ... and having a **fixed number of data slots** may lead to unnecessary waste or packet drops

# Framed ALOHA with reservation frame and data slots

Create a short reservation FRAME with  $S_R < K$  slots

1. An **active user** selects one of them at random (possibility of collision)
2. The  $S \leq S_R$  successful devices are granted a dedicated data slot
3. The data phase consists of  $F = S$  slots, which is dynamically adjusted
  - Recall: Flexibility requires signaling



In absence of reservation frame, users perform grant-free access and apply random access in the data frame.

If  $K$  is known, how long should  $S_R$  be?



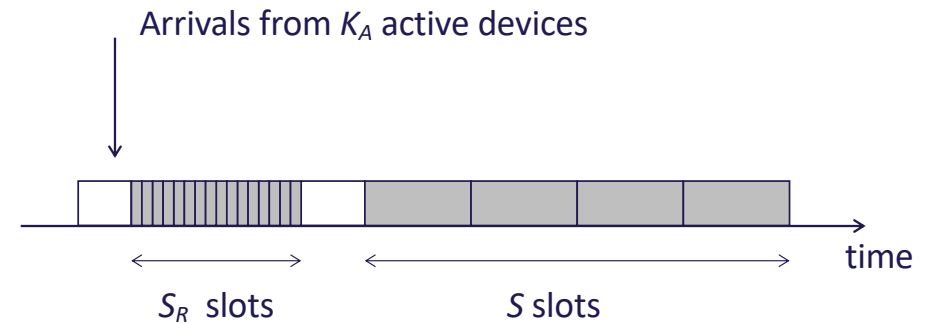
# Framed ALOHA: Size of the reservation frame

Let  $K_A$  be the number of active devices

**Probability of a successful transmission in a given slot =** the probability that **any** of the devices selects this **particular** slot while **others** do not

$$P(K_A) = \binom{K_A}{1} \frac{1}{S_R} \left(1 - \frac{1}{S_R}\right)^{K_A-1}$$

A simple maximization of this expression w.r.t.  $S_R$  leads to  $S_R = K_A$



# Framed ALOHA: Dependence on # of active devices

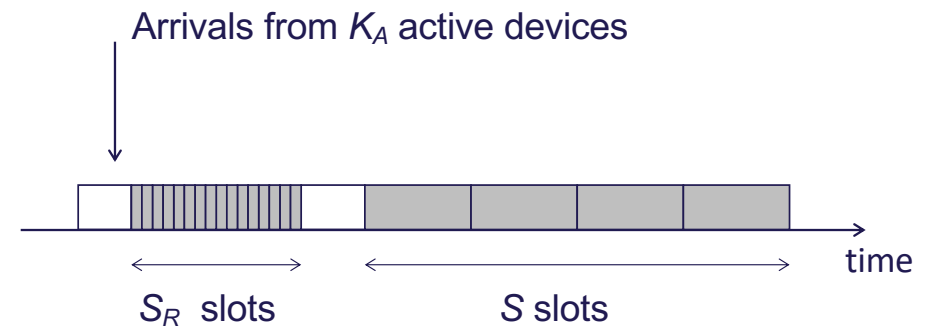
We have assumed that Basil knows  $K_A$

- Still does not know **which**  $K_A$  devices
- In practice,  $K_A$  should be estimated

Optimized success probability

$$P(K_A) = \left(1 - \frac{1}{K_A}\right)^{K_A-1}$$

approaches  $e^{-1}$  as  $K_A$  goes to infinity



# Framed ALOHA: Estimating # of active devices

Relation among the average numbers of active  $\bar{K}_A$ , newly arrived  $\bar{K}_N$  and retrying/collided  $\bar{K}_C$

$$\bar{K}_A = \bar{K}_N + \bar{K}_C$$

For large numbers we can remove the bars and work with the average values as if exact

$$K_A = K_N + K_C$$

In a stationary regime

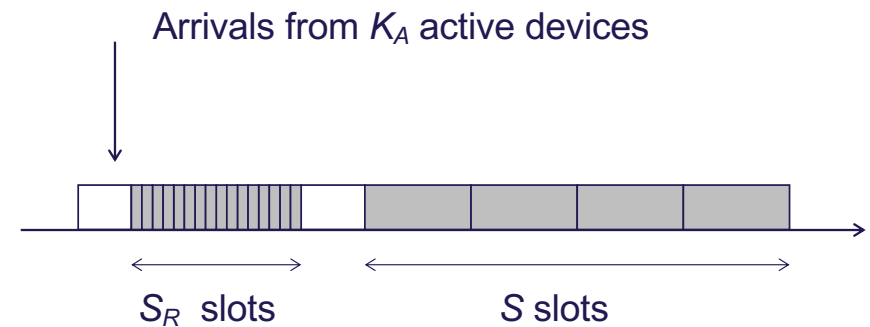
$$K_C = K_A(1 - P(K_A)) \approx K_A(1 - e^{-1})$$

such that the relation between new and active is

$$K_A = K_N \cdot e$$

Throughput (=goodput)

$$G = \frac{K_N}{K_A T} = \frac{K_A e^{-1}}{K_A T} = \frac{e^{-1}}{T} \quad [\text{packet/s}]$$

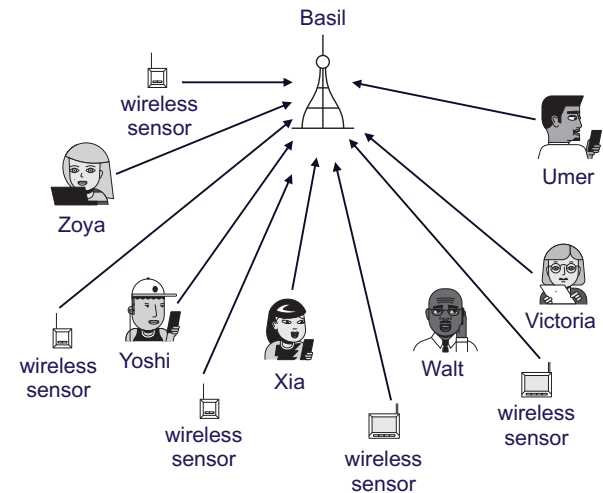


In the book it is shown how to take into account past collisions for throughput calculation

**But can we use the knowledge/memory of past collisions to get more efficient access?**

# Probing

For framed ALOHA we (optimistically) assume that  $K_A$  is known or at least a *good* estimate is available



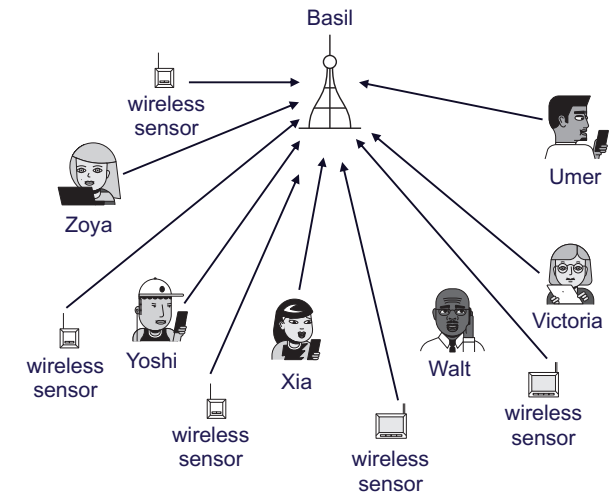
Back to the cartoon from this chapter

- People in the dark room do not know each other, otherwise a predefined contract or hierarchy could be used
- Walt says “one of you come out of the room”, but who feels entitled to be “the one”?
- The question of Walt is in fact probing, not scheduling

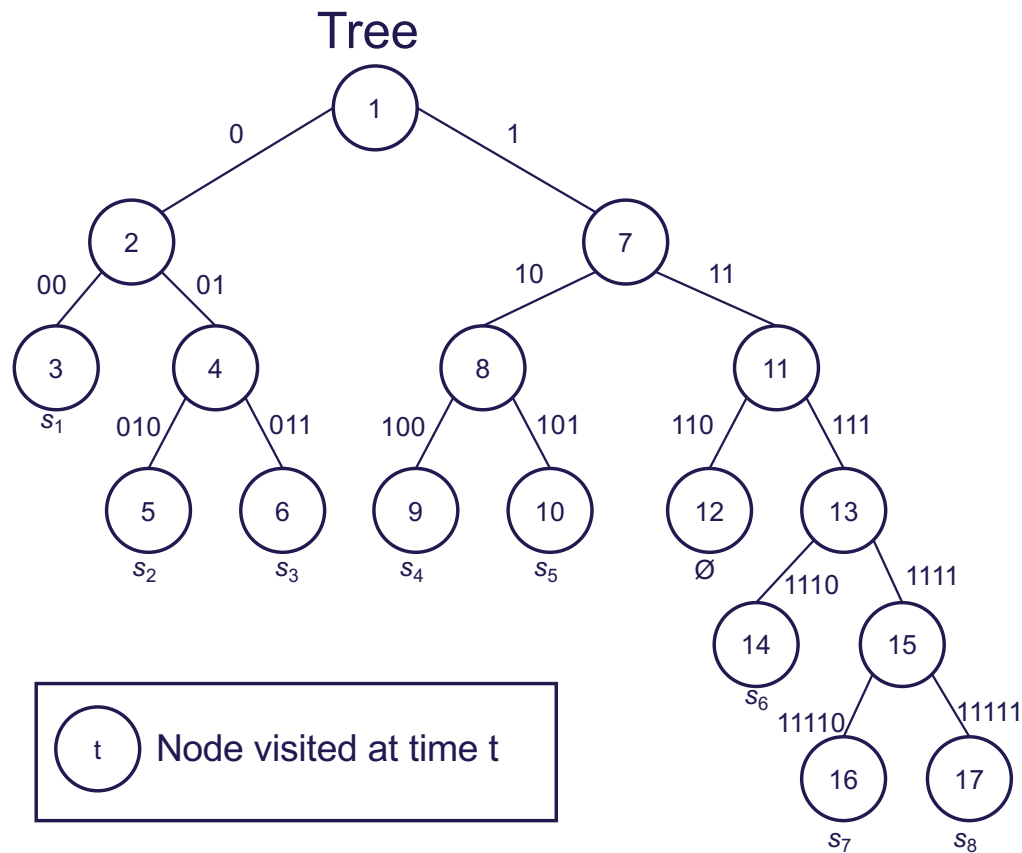
# Probing/polling

## Probing/polling mechanism

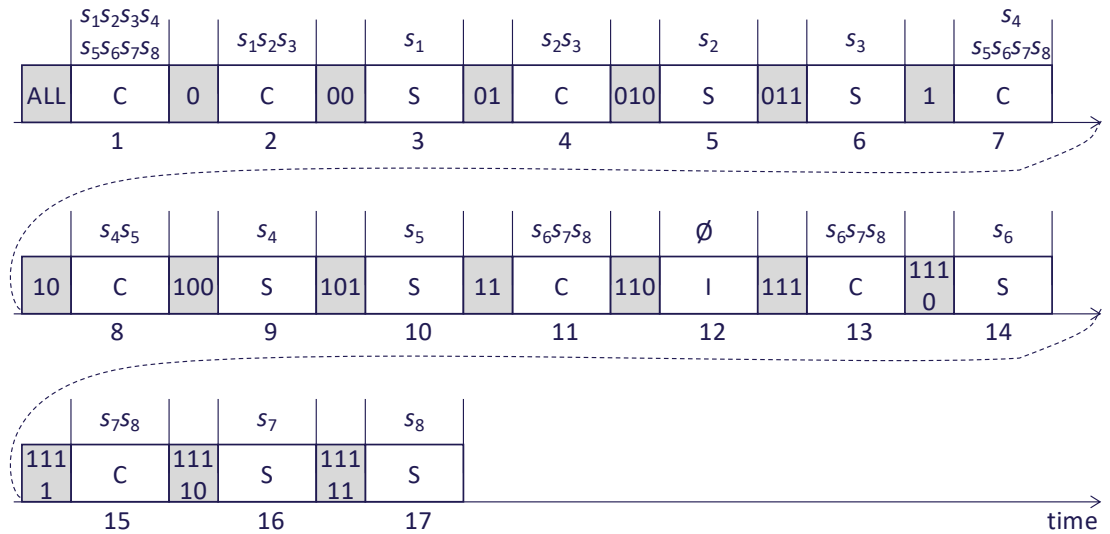
1. Basil probes by sending an invite message
2. The  $K_A$  devices with data respond
  - if**  $K_A = 0$  no new packets and the data phase is idle; BS goes back to 1
  - else if**  $K_A = 1$  there is no collision; device will be assigned a data slot
  - else**  $K_A > 1$  collision occurs; polling is initiated



# Probing: Example for $K_A = 8$

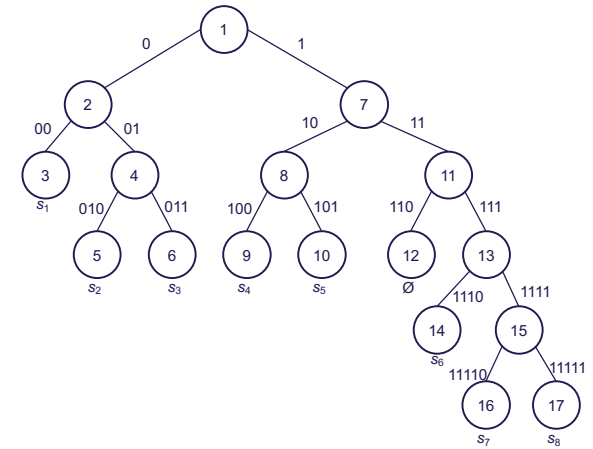


Tree in time: collision (C), single (S), idle (I)



# Remarks on probing

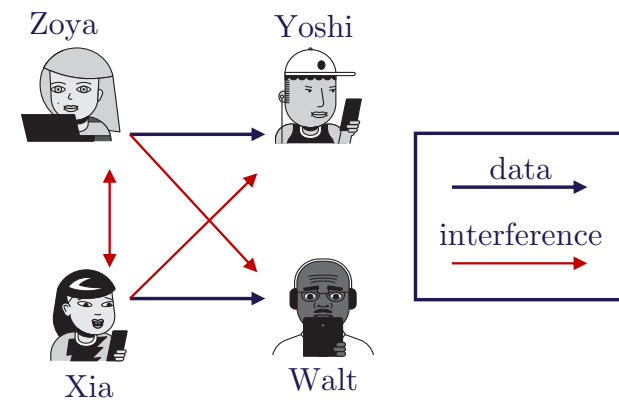
- Instead of randomization, the devices can use unique addresses for probing
- Probing process allocates short ad hoc addresses to the active devices
- Using of a feedback (collision, single, idle) instead of a probe offers equivalent traversal of the tree
- Combining ALOHA and probing
  - ALOHA uses memoryless randomization
  - Probing retains memory



# Carrier sensing

The problem of **spectrum sharing** requires also randomization

- Proximate links that share the same channel may cause interference
- Lack of coordination among links that are not logically connected and can only communicate through interference
- Example: the Wi-Fi access points of two neighbors

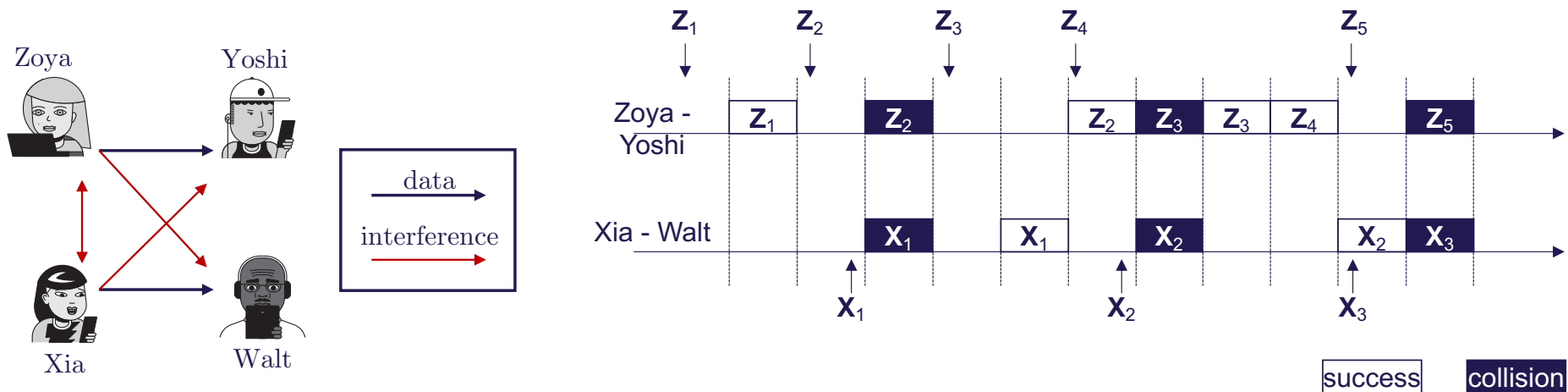




# Carrier sensing

Spectrum sharing with a slotted synchronized structure

- Questionable to assume that two independent systems are a priori synchronized, but synchronization can occur through the access of a shared medium
- New packets **always need to wait** at least until the start of a new slot
- Enforced **waiting synchronizes the packets to collide**



# Carrier Sense Multiple Access (CSMA)

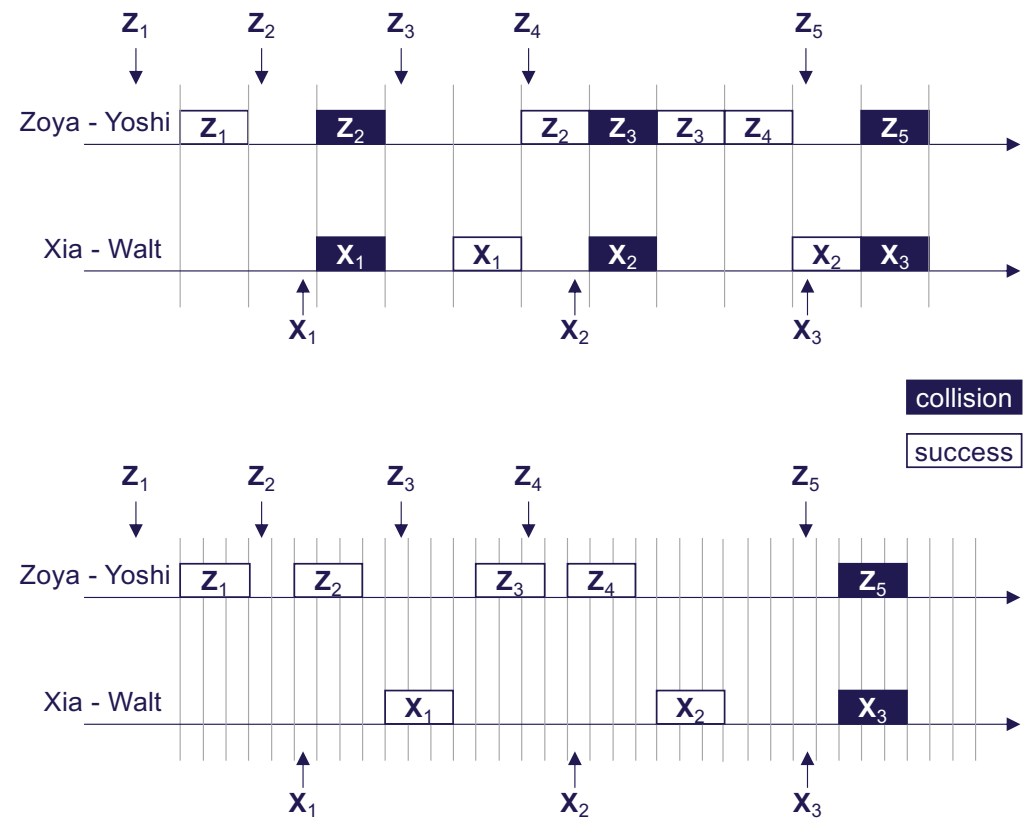
**Idea:** Make the *idle slots* short (cheap!)

Finer time resolution  
**preserves asynchronism** of arrivals

Devices not currently transmitting  
 must listen to **sense** if carrier is free

- If the medium is busy,  
 device waits for a random time  
 =  
 countdowns  
 a random number of idle minislots

**Carrier sensing** obviates the need  
 for fixed-length packet



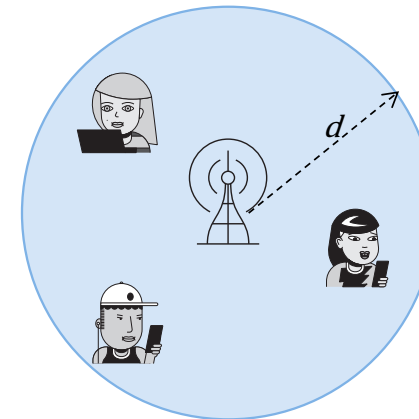
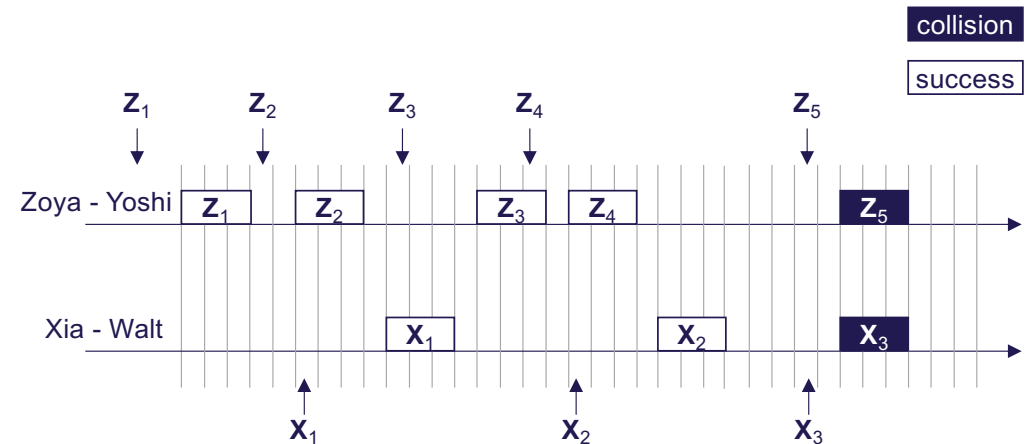
# Elements of CSMA

Random number of waiting minislots

- Pausing countdown during sensed carriers to avoid aligning of the access instants after the medium is sensed idle

Choosing the idle slot size

- Carrier should be reliably detectable
- Propagation delay  $T_I = \frac{d}{c}$  or  $T_I = \frac{2d}{c}$  if the sensing range is larger than the communication range



# Feedback to the transmitter

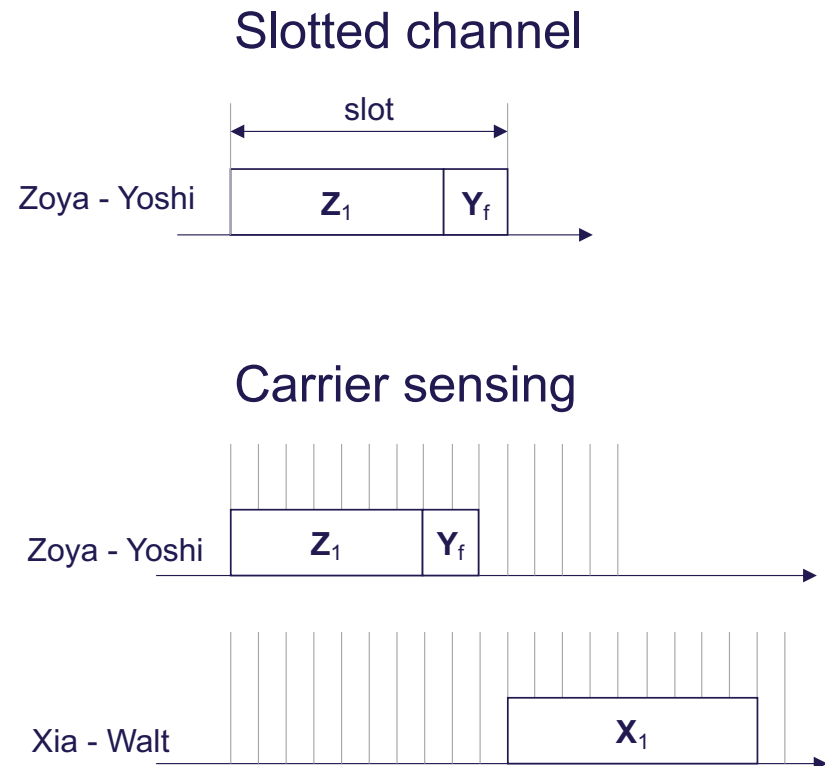
The possible outcomes:  
**collision** and **success**

The transmitter must be informed of the outcome through **feedback**:

- Acknowledged (**ACK**)
- Not acknowledged (**NACK**)

Implemented differently  
in a slotted channel  
and in carrier sensing.

In carrier sensing,  
Yoshi's feedback can **skip sensing**,  
making it **HIGH** priority

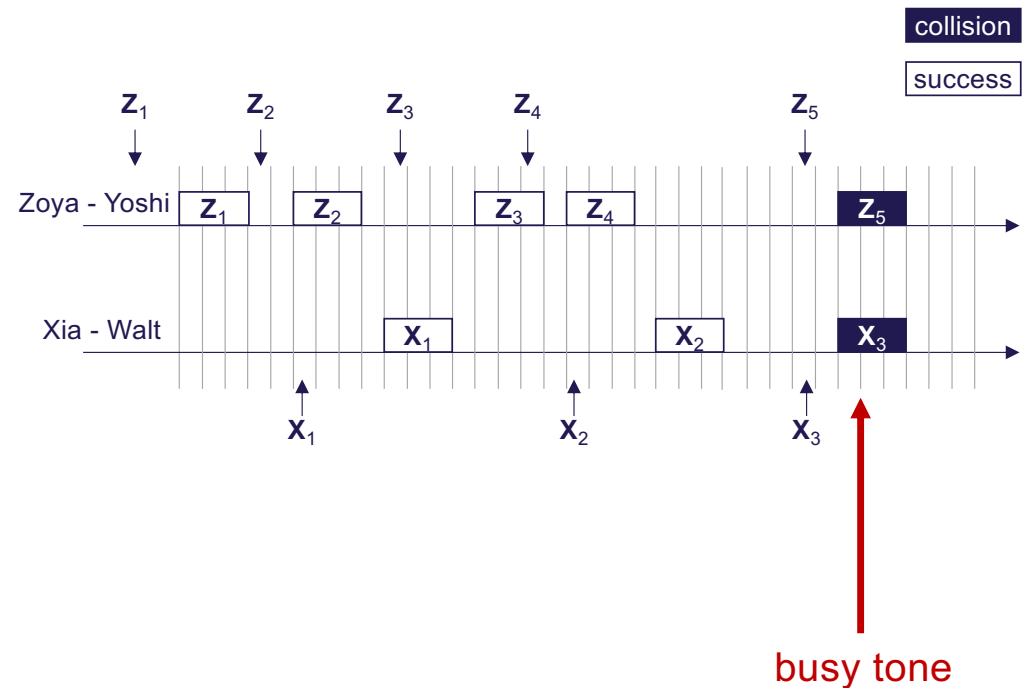


# Feedback to the transmitter

Idle slots are basis for different prioritization levels:

- Users of a given priority need to wait for a priority-dependent number of idle slots
- Malicious users could exploit this

Full-duplex and used of busy tones



# Carrier sensing and multiple hops

Hidden terminal

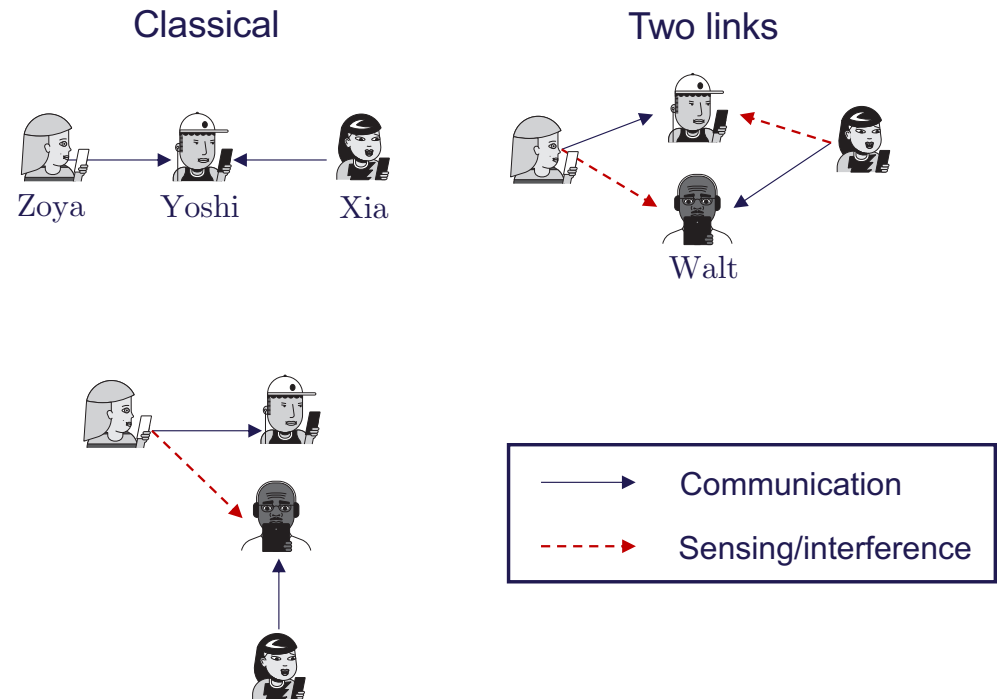
Potential **weakness** of carrier sensing: assuming that everyone can hear everyone else.

Actual setup is rarely single-hop

## Hidden terminal problem:

The carrier seems to be idle when it is actually being used

- ✓ Could be tackled by an increased sensing range



Two links, but one receiver is a victim

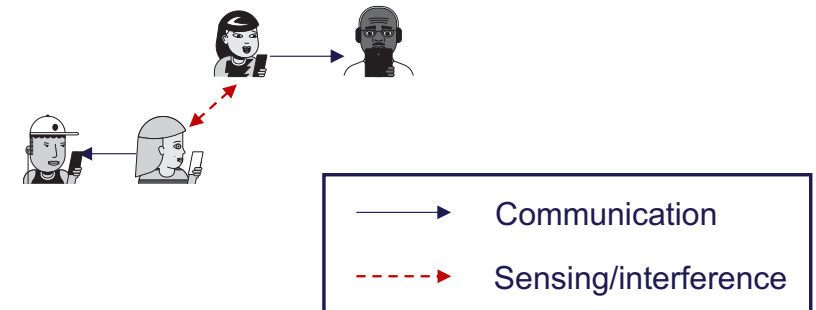
# Carrier sensing and multiple hops

## Exposed terminal problem:

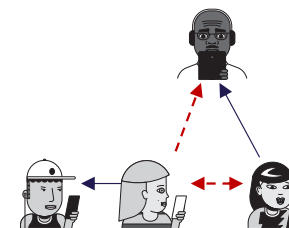
The carrier seems busy when it is not and a transmission can be carried out

There are multi-hop setups in which sensing still works well

Exposed terminal



Sensing works



# Carrier sensing and multiple hops

Short reservation packets can make collisions cheaper

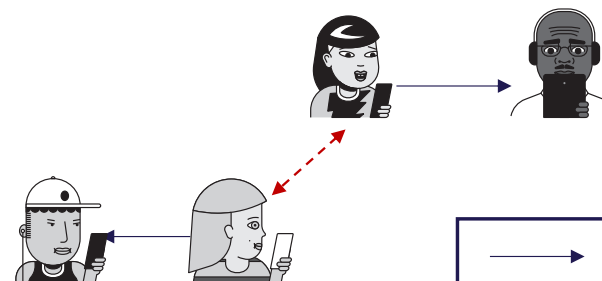
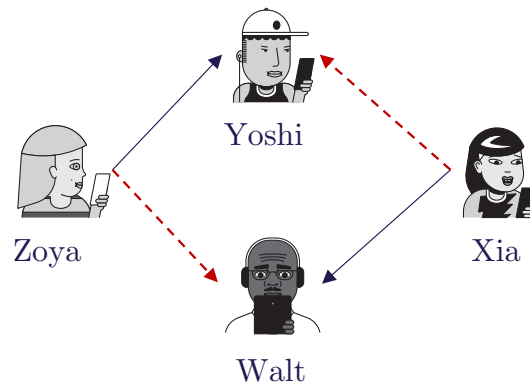
First, Zoya transmits a *Request-to-send (RTS)* to Yoshi

Then, Yoshi responds with a *Clear-to-send (CTS)* to Zoya.

CTS signals potential interferers to refrain from transmitting because the medium will soon be busy

**Hidden terminal:** Xia receives CTS

**Exposed terminal:** Xia only receives RTS





# Outlook and takeaways

## Random access protocols

**ALOHA:** memoryless randomization, useful for sporadically active devices

**Probing:** collision resolution with memory based on tree splitting  
Related to Group Testing (COVID-19!)

**Carrier sensing** makes the idle slots cheap

**Multi-hop** scenarios bring the issues of hidden/exposed terminals